

Thermodynamic and Transport Properties of Hydrogen and Deuterium Fluids within Atom-Atom Approximation

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ABSTRACT

Computer simulation results for highly compressed molecular hydrogen and deuterium fluids at pressures up to 100 GPa are presented. Non-empirical atom-atom approximation for non-rigid molecules was used for description of intra- and intermolecular interactions. Quantum corrections are included within the Feynman variational approach. Pressure, energy, isothermal compressibility, thermal expansion, heat capacities, speed of sound, as well as transport properties of hydrogen and deuterium fluids at elevated temperatures and high densities are computed using appropriate computer simulation procedures. Predictions of self-diffusion, shear viscosity and heat conductivity of shock-compressed deuterium and hydrogen fluids are presented.

KEY WORDS: atom-atom potentials; computer simulation; deuterium; heat capacity; heat conductivity; high density; molecular hydrogen; self-diffusion; viscosity.

1. INTRODUCTION

Structure, thermodynamic and transport properties of hydrogen isotopes in the condensed phase have been studied intensively for many years. A rich body of experimental material in the cryogenic [1] as well as in high-temperature [2,15] regions has been accumulated. At high pressures the most important experimental results have been obtained in the solid phase by the diamond anvil method [3].

Fluid hydrogen isotopes at intermediate temperatures remain much less investigated. The existing published data has yielded the equation of state for the solid state [5] and for the fluid phase of normal hydrogen at temperatures up to 500 K and pressures up to 2 GPa [4]. Between the high-temperature and high-pressure dynamic shock-compression data and that low-temperature limit no experimental studies were performed. The transport properties of hydrogen or deuterium fluids in this region of high density and elevated temperatures are almost unknown.

Since it is quite difficult to do an experiment here, it is of particular urgency to undertake a theoretical prediction of the properties of highly compressed fluid hydrogen. However, there is an extremely restricted choice of non-empirical methods of predicting the properties of such dense systems. Methods based on the direct quantum-mechanical computer simulation, e.g., the path-integral Monte Carlo (PIMC) method [6], are very demanding of computational resources and have not yet attained the necessary accuracy.

There are certain difficulties in applying to hydrogen the well-developed methods of the theory of liquids, which make use of the model of rigid, impermeable molecules. The absence of closed atomic electronic shells makes hydrogen extremely compressible and stable at once in condensed phase. The softness of intermolecular repulsion in

hydrogen becomes very important at high densities. It is just what makes hydrogen different from many other substances, and therefore the well-known and useful molecular models like hard spheres or dumbbells could not be applied to hydrogen without essential modification.

The difficulties facing the theoretical prediction of the properties of highly compressed hydrogen are also due to the appreciable quantum effects [5]. Non-rigidity effects, which play an important role in highly compressed fluid hydrogen at high temperatures [7,9], remain substantial at intermediate temperatures as well, especially near the line of crystallization, where the density of the fluid is high. In this region, one cannot also neglect quantum effects, particularly for the light isotopes of hydrogen. The goal of the present study is to investigate the possibility of using the approximation based on atom-atom potentials (AAP) [9] in order to predict the behavior of thermophysical properties of dense hydrogen at intermediate temperatures and high densities.

2. *AB INITIO* ATOM-ATOM POTENTIALS

In the AAP approximation [7,9], the energy of interaction of hydrogen molecules is expressed in terms of the interaction energy of individual pairs of atoms. Two hydrogen atoms interact differently depending on their total spin. In the singlet ground state the atoms form an H_2 molecule - a bound $^1\Sigma$ state with a well depth of about 4.75 eV and a bond length of 0.74 Å. In the triplet excited state $^3\Sigma$ the curve of the interaction energy does not have a minimum (except for a small dispersion well at a distance greater than 3 Å).

In the AAP approximation, the intermolecular interaction energy can be expressed relatively simply in terms of the interaction energy of the atoms within the

molecule. This approximation is based on the Bohm-Alrichs theorem, which was proved by those authors in Ref.[8] in the Hartree-Fock approximation, in which the molecular orbitals are represented by a linear combination of atomic orbitals (LCAO MO). According to the theorem, the energy of the non-valent interaction of two atoms (i.e., the interaction energy of two atoms belonging to different molecules with closed electronic shells) is equal to the weighted average (i.e., with allowance for the degeneracy with respect to projections of the spin and orbital angular momenta) of the interaction energy of two free atoms calculated in this same approximation.

According to the theorem, the non-valent interaction potential $\phi(r)$ of hydrogen atoms can be calculated as a linear combination of the singlet and triplet potentials, with weights proportional to the multiplicities of these states:

$$\phi(r) = \frac{1}{4}U(^1\Sigma|r) + \frac{3}{4}U(^3\Sigma|r). \quad (1)$$

Here $U(^1\Sigma|r)$ is the interaction energy of two atoms in the $^1\Sigma$ ground state (with antiparallel spins); $U(^3\Sigma|r)$ is the interaction energy of atoms in the $^3\Sigma$ excited state (with parallel spins).

Within AAP approximation the total energy of two H_2 molecules found in their ground electronic states consists of intra- and intermolecular contributions:

$$U_2 = U(^1\Sigma|R_{12}) + U(^1\Sigma|R_{34}) + \phi(r_{13}) + \phi(r_{14}) + \phi(r_{23}) + \phi(r_{24}). \quad (2)$$

The indices 1 and 2 refer to the atoms bound together in the first molecule, while 3 and 4 refer to the atoms bound in the second molecule. Here and below $R_{ij} = R_{12}, R_{34}, \dots$ are the intramolecular interatomic distances (the instantaneous lengths of the chemical bonds in the molecules), while $r_{ij} = r_{13}, r_{14}, \dots$ denote the instantaneous distances between atoms of different molecules (intermolecular distances).

For N atoms ($N/2$ molecules) the generalization of Eq. (2) is written

$$U_N = \sum_{\text{intra}} U(^1\Sigma | R_{ij}) + \sum_{\text{inter}} \phi(r_{ij}). \quad (3)$$

The first sum in (3) is over the intramolecular interactions of all $N/2$ molecules, and the second sum is over all the $N(N-1)/2$ pairs of atoms belonging to different molecules.

Eq.(3) is applicable to any spatial distribution of atomic centers if an additional rule for the selection of bonded atomic pairs (chemical bonds localization) is adopted. We applied the following algorithm [9]. The first pair at given specific configuration of N atoms is taken to be that which have the shortest interatomic separation. Excluding these two atoms, the next pair is taken to be that having the shortest interatomic distance amongst the remaining $N-2$ atoms *etc.* until all the atoms have been exhausted.

We applied the following analytical approximation for the ground $^1\Sigma$ state [9]:

$$U(^1\Sigma | R) = D_e [\exp(-2x) - 2\exp(-x) - ax^3(1-bx)\exp(-cx)], \quad (4)$$

where $x = 1.4403(r/r_e - 1)$, $r_e = 0.74126 \text{ \AA}$, $D_e/k = 55088 \text{ K}$, $a=0.1156$, $b=1.0215$, $c=1.72$. Eq.(4) gives an excellent approximation of the $^1\Sigma_g^+$ -curve within a wide range of distances (0.3-5 \AA). The nonvalent interaction potential $\phi(r)$ was represented in the approximation proposed by Saumon and Chabrier[13]:

$$\phi(r) = \varepsilon [\gamma \exp\{-2s_1(r-r^*)\} - (1+\gamma)\exp\{-s_2(r-r^*)\}]. \quad (5)$$

The parameters appearing in Eq.(5), $r^* = 3.2909 \text{ \AA}$, $\varepsilon = 1.74 \cdot 10^{-3} \text{ eV}$, $\gamma = 0.4615$, $s_1 = 1.6367 \text{ \AA}^{-1}$, and $s_2 = 1.2041 \text{ \AA}^{-1}$, were obtained in Ref. [13] on the basis of the well-known variational calculations of Kolos and Wolniewicz for the H_2 molecule[10]. Eq.(5) also gives a very accurate description of potential (1) over a wide interval of distances (from 0.5 to 3.5 \AA), including the region of strong repulsion at short distances and the region of weak dispersional attraction at large distances.

Thus, the AAP approximation (1)-(3) with the potentials (4) and (5) permits a quite simple determination of the potential surface of the ground state of a system consisting of an arbitrary number of hydrogen molecules. We note that this approximation does not contain any adjustable parameters found from the experimental data but uses only the pair potentials $U(^1\Sigma |R)$ and $U(^3\Sigma |R)$ obtained from *ab initio* calculations [10].

A comparison of the predictions of the AAP approximation with the results of direct quantum-mechanical calculations of the H_2-H_2 interaction energy and with the results of experiments on the scattering of molecular beams has shown [7] that this approximation gives an entirely satisfactory description of the short-range repulsion of the molecules but that the molecular attraction at large distances is overestimated somewhat [12]. At large intermolecular distances, the AAP approximation does not recover also the asymptotic behavior of the orientational part of the intermolecular potential, in particular, that of its quadrupole-quadrupole component. This shortcoming, which is important at relatively low densities, can also be important in the description of some phase transitions in solid hydrogen [5]. At the same time, at high pressure in the isotropic phase, where the main role is played by the short-range repulsive forces, this aspect of the AAP approximation plays a secondary role.

3. QUANTUM CORRECTIONS

For predicting the thermodynamic behavior of dense deuterium and especially hydrogen at lower temperatures on the basis of the AAP approximation, we modified this approach to incorporate quantum-mechanical effects, which play a governing role in the behavior of these light molecules at low temperatures. We adopted [12] the

approach proposed by Feynman, which is based on his variational procedure for the free energy [11].

In this approach the free energy of a quantum-mechanical particle in an external field can be calculated approximately by a classical method if its potential energy $V(r)$ is replaced by a certain effective potential given by

$$\tilde{U}(r, T) = \frac{1}{\sqrt{\pi}} \int_{-\infty}^{+\infty} V(r + \lambda t) \exp(-t^2) dt. \quad (6)$$

The parameter

$$\lambda = \hbar / \sqrt{6mkT} \quad (7)$$

plays the role of the quantum-mechanical wavelength associated with the given particle; k is Boltzmann's constant.

In the simplest cases, the quantum corrections to the potential within approximation (6) are easily calculated explicitly. As was shown in Ref. [12], considering quantum effects in the framework of the Feynman approach reduces simply to some increase in the effective interatomic repulsion. A rough estimate of the possible influence of these effects on the repulsion of the atoms was made by taking into account that the parameter b is close to 2 (a.u.)^{-1} for many atoms [7]. For example, for deuterium at $T = 500 \text{ K}$ the increase in the repulsion is only around 2.5%, but for hydrogen at $T=200 \text{ K}$ it is already about 20%.

As to the intramolecular vibrations, their quantum character is manifested at much higher temperatures, so that a quantum correction becomes comparable to the heat capacity itself at temperatures below 1000 K. In view of this (while remaining formally within the framework of the Feynman approach), we replaced the first-order quantum correction to intramolecular energy by the exact expression for harmonic oscillator

[12]. At high temperatures, it goes over to the original Feynman approach, and at low temperatures, it gives the exact expression for the harmonic-oscillator contribution to the free energy and the other thermodynamic properties.

Thus one can assume that in the investigated temperature interval, taking quantum effects into account in the intermolecular interaction can be done at the level of a correction to the intermolecular potential, and the Feynman variational approach [11] can be completely applicable to highly compressed hydrogen isotopes at temperatures higher than ambient.

4. MONTE CARLO SIMULATION

To predict the equilibrium properties of fluid hydrogen on the basis of the AAP approximation with the quantum corrections introduced above, we chose the method of Monte Carlo simulation. The calculation was done in an NVT ensemble, with N hydrogen atoms placed in a rectangular cell with periodic boundary conditions. The size of the cell was determined by the specified density $n = N/V$, and the initial configuration corresponded to a random distribution of molecules with bond lengths close to the equilibrium bond length R_e . Each step of the experiment included a random choice of an individual atom, for which an attempt was made to move it to a new position within a specified distance δ . Discrimination of the steps was carried out by the standard Metropolis method [14]. The value of δ was chosen such that around 40% of the steps were successful. It took about 1000 successful steps/atom to establish the equilibrium distribution. Probable errors were estimated by standard statistical methods for a significance level of 0.05.

The isothermal compressibility, the thermal pressure, and the isochoric heat capacity C_V were computed along with the pressure and the total energy [12]. The

calculations were performed for $N = 256$ or $N = 500$ atoms in the cell (128 and 250 H_2 or D_2 molecules in the cell, respectively). The interatomic interaction potential was ‘cut off’ at a distance $r_{max} = 5 \text{ \AA}$; this did not introduce any new errors of practical consequence.

5. MOLECULAR (ATOMIC) DYNAMICS PROCEDURE

In order to predict transport properties of dense fluid hydrogen, we examined a classical system of N atoms forming non-rigid homonuclear diatomic molecules. The method applied is similar to the well-known molecular dynamics method [16], except the structure element chosen. We consider the separate atoms in molecules within classical mechanics as elements of structure and performed such *atomic dynamics* (AD) simulation at constant number of atoms N , volume V and energy E (*NVE*-simulation) with periodic boundary conditions. Newton equations of atomic motion have been integrated using the simplest three-point algorithm described by Norman *et al.* [16]. Low masses of hydrogen isotopes along with high frequencies of intramolecular vibrations and strong intermolecular forces require relatively short time steps in numerical integration of equations of motion.

The time step Δt ranged from 0.0001 picosecond (10^{-16} s) at relatively high temperatures and densities up to 0.001 picosecond (10^{-15} s) at lower temperatures and/or densities. Larger values of Δt speed up the equilibration (relaxation) period in AD-simulation but require special efforts for maintaining the desired temperature. We applied correction factors to all velocities during relaxation period, preceding the main AD run to keep temperature close to the given value, and also checked the correspondence between atomic velocities, center-of-mass velocities, and the Maxwell’s distribution.

We used 'near-equilibrium' atomic distributions generated in our Monte Carlo simulations as starting atomic configurations and after Maxwell equilibrium distribution was reached, we computed self-diffusion D , viscosity η and heat conductivity κ and corresponding velocity, shear-stress and heat-flux autocorrelation functions (ACF). We also calculated interatomic and intramolecular distribution functions. All results presented below are averaged values over 1000 runs of 0.2 picoseconds each. Every set of runs took from 100 up to 200 hours on PC (in background).

6. RESULTS AND DISCUSSION

6.1. *Thermodynamic functions.*

The results of MC computer simulation and the data obtained in Ref.[4] are in quite good agreement, overall (see Table 1). The only disagreement is that the calculated pressure of the fluid hydrogen is somewhat (about 0.2 GPa) lower than experiment, even when the quantum corrections are taken into account [12]. This is apparently due to the aforementioned characteristic overestimate of the attraction of the molecules at large distances in the AAP approximation [9].

As expected, quantum effects particularly influence the isochoric heat capacity over the entire investigated temperature interval. The corrections to the thermal expansion coefficients and sound velocity are less important, but even for them the agreement with experiment is improved when these corrections are taken into account. As the temperature increases, this agreement becomes better and better, although even for $T=200$ K the predictions remain satisfactory. It is seen that the quantum corrections in the given temperature interval give approximately the same contribution to the pressure (of the order of 10%) as the typical value of the intramolecular contribution [9] due to the non-rigidity of the hydrogen molecule. Considering the quantum corrections

is necessary not only in calculating the heat capacity but also the thermal expansion, and it substantially improves the agreement with experiment, especially at low temperatures. For an approach that does not contain even one adjustable parameter, the agreement can be considered completely satisfactory.

6.2. Transport properties.

In Table 2, we present the predicted pressures and transport properties of fluid hydrogen at high densities and different temperatures. The simulation results are compared here also to shock-compression data [2,15].

Self-diffusion coefficients D have been estimated in three ways: 1) from the long-time slope of the mean-square atomic displacement, 2) as integrals of time-dependent atomic velocity ACF, and 3) as integrals of time-dependent molecular center-of-mass velocity ACF. All approaches give the same result within estimated error limits. The computation of shear viscosity and thermal conductivity is computationally more time consuming (it requires much more runs in AD-simulation) but is only technical difficulty. Unfortunately, we do not know any measured or predicted values of transport coefficients at shock-compression conditions to compare our predictions with. The estimated statistical error of predicted shear viscosity and thermal conductivity is still significant, but the more precise prediction is beyond powers of AD simulation on available PC and requires high-performance computer.

6.3. Velocity autocorrelation functions.

In Fig.1 and 2 we present the time-dependent atomic ACFs along with molecular center-of-mass (dot line) velocity ACF at low and high temperatures. There is a pronounced fine oscillation structure of the atomic velocity ACF while the time dependence of the molecular center-of-mass velocity ACF is smooth and quite usual for

simple liquids at high densities. The period of those oscillations is close to the period of intramolecular vibration [17]. It is clear, that highly compressed molecular fluid, composed from non-rigid molecules, will behave like a system of strongly coupled oscillators. The ACF oscillations are much more pronounced at higher densities and lower temperatures. The higher the temperature is, the more damped the ACF oscillations are.

7. CONCLUSIONS

The predictions of the AAP approximation are in reasonable agreement with the existing experimental data both at moderate and at high temperatures, in spite of the fact that the AAP potentials do not explicitly contain contributions from the short-range multiparticle and long-range electrostatic intermolecular forces and that the electronic excitation of the molecules is not fully taken into account [7,9].

Quantum corrections introduced to the AAP approximation [12] provide the possibility to calculate the thermodynamic properties and structure parameters of fluid hydrogen at high pressures, beyond the limits of the experimentally investigated region.

The temperature and density dependence of self-diffusion in fluid hydrogen predicted within AAP approximation was examined in Ref.[17]. Self-diffusion coefficient demonstrates very slow decrease with compression in contrast with predictions of the hard-sphere model. The temperature dependence of D is rather gas-like (power) than inverse-exponential one, typical to the activation mechanism of diffusion. Our simulations have also shown that the time-dependent atomic autocorrelation functions in diatomic fluid had fine oscillation structure, more pronounced at lower temperatures and higher compressions.

Both Enskog and Frenkel approaches fail to describe the simulated density and temperature dependence of self-diffusion coefficients in dense fluid hydrogen (see Ref. [17] for details). It is not surprising because the hydrogen inter-atomic repulsion, as was mentioned above, is very soft. The $\log(nD) - 1/T$ -dependence is far from linearity, in contrast to Frenkel's activation theory. At the same time the slope of $\log(nD) - \log(T)$ dependence is nearly constant [17] and changes with density from values close to $\frac{1}{2}$ (corresponding to the known ideal-gas law) up to 1.5 and more. Unfortunately, the inaccuracy of our shear viscosity and heat conductivity predictions makes them inconclusive in respect of suitability of existing theories for highly compressed hydrogen fluid.

Of course, such simple model as AAP approximation cannot pretend to complete description of dense hydrogen. At least two important effects have been omitted in the present calculations. Firstly, using atom-atom models means that the effects of electronic polarisability and long-range forces are not correctly treated. Secondly, we have ignored electronic excitations, leading in the end to the metallization of hydrogen at higher densities and to the dissociation at higher temperatures.

Although the AAP approximation does suffer from the list of shortcomings mentioned above, as a non-empirical approach this approximation has its indisputable advantages and its own sphere of application. This approach requires a minimum of initial information for predicting the properties, makes it possible to describe the effects of molecular non-rigidity, and can be useful for predicting not only of thermodynamic behavior of molecular fluids at high pressures but also of the diffusion, viscosity, and other transport properties of compressed fluids.

REFERENCES

1. B. I. Verkin (ed.), *Properties of Condensed Phases of Hydrogen and Oxygen*, Naukova Dumka, Kiev (1984) [in Russian].
2. S. T. Weir, A. C. Mitchell, and W. J. Nellis, *Phys. Rev. Lett.* 76:1860 (1996).
3. H. K. Mao and R. J. Hemley, *Rev. Mod. Phys.* 66: 671 (1994).
4. A. A. Sheuinina, N. G. Bereznyak, V. P. Vorob'eva, and M. A. Khadzhmuradov, *Low Temp. Phys.* 19: 356 (1993).
5. V. G. Manzhelii and Yu. A. Freiman (eds.), *Physics of Cryocrystals*, AIP Press, Woodbury, New York (1996).
6. B. Militzer, W. Magro, and D. Ceperley, *Contr. Plasma Physics* 39:151 (1999).
7. E. S. Yakub, *Low Temp. Phys.* 20: 579 (1994).
8. H.-J. Bohm and R. Ahlrichs, *J. Chem. Phys.* 77: 2028 (1982).
9. E. S. Yakub, *Physica* B265: 31 (1999).
10. W. Kolos and L. Wolniewicz, *J. Chem. Phys.* 41: 3363 (1965); 43: 2429 (1966).
11. R. P. Feynman and A. R. Hibbs, *Quantum Mechanics and Path Integrals*, McGraw-Hill, New York (1965).
12. E. S. Yakub, *Low Temp. Phys.* 26: No. 4, (2000) (in press).
13. D. Saumon and G. Chabrier, *Phys. Rev.* A44: 5122 (1990).
14. N. Metropolis *et al.*, *J. Chem. Phys.* 21: 1087 (1953).
15. N.C.Holmes, M.Ross, and W.J.Nellis, *Phys. Rev.*, B52 (1995) 15835.
16. G.E.Norman, V.Yu.Podlipchuk, and A.A.Valuev. *J. Moscow Phys. Soc.*, 2:7 (1992).
17. E. S. Yakub, *J. Molec.Liquids*, (2000) (in press).

Table 1.

Predicted (MC) and experimental [4] pressures P , isochoric C_V and isobaric C_p heat capacities, thermal expansion α_T and isothermal compressibility β_T and speed of sound a of fluid hydrogen on the $P = 2$ GPa isobar at $T = 200$ K ($V = 11.17 \text{ cm}^3 \text{ mol}^{-1}$, $\lambda = 0.20 \text{ \AA}$), $T = 300$ K ($V = 11.63 \text{ cm}^3 \text{ mol}^{-1}$, $\lambda = 0.16 \text{ \AA}$), and $T = 500$ K ($V = 12.53 \text{ cm}^3 \text{ mol}^{-1}$, $\lambda = 0.13 \text{ \AA}$)

T	(K)	200		300		500		$\Delta^*)$
		MC	[4]	MC	[4]	MC	[4]	
P	(GPa)	1.81	2.00	1.75	2.00	1.72	2.00	0.01
C_V/R		2.84	2.98	3.22	3.24	3.12	3.14	0.03
C_p/R		3.26	3.62	3.62	3.64	3.56	3.68	0.05
α_T	(10^{-3} K^{-1})	0.48	0.42	0.37	0.39	0.32	0.36	0.03
β_T	(GPa^{-1})	0.15	0.15	0.15	0.16	0.18	0.18	0.02
a	(km s^{-1})	6.59	6.40	6.59	6.38	6.34	6.37	0.05

^{*)} estimated statistical error of MC simulation, $N = 256$

Table 2.

Predicted pressures and transport coefficients of hydrogen and deuterium fluids

Isotope	N _a	T	V	P	Predicted			
					P _{MC}	D _{AD}	η _{AD}	κ _{AD}
		(K)	(cm ³ mol ⁻¹)	(GPa)	(GPa)	(10 ⁻⁸ m ² s ⁻¹)	(10 ⁻⁴ Pa s)	(W m ⁻¹ K ⁻¹)
H ₂	256	300	11.63	2.0 ¹⁾	1.72 ⁴⁾	2.89±0.04	0.48±0.20	1.09±0.37
H ₂	256	500	12.53	2.0 ¹⁾	1.75 ⁴⁾	6.22±0.06	0.56±0.09	1.14±0.18
D ₂	500	2275	3.44	100 ²⁾	107.4	4.08±0.04	5.30±1.07	5.32±1.20
D ₂	256	2820	7.98	12.0 ³⁾	12.9	13.54±0.09	1.26±0.21	1.71±0.24
D ₂	500	3910	4.51	52.5 ³⁾	59.8	11.3±0.1	2.9±0.7	3.4±0.8
D ₂	256	4660	7.02	22.6 ³⁾	22.2	20.1±0.14	1.5±0.3	2.9±0.35

¹⁾Ref.[4] ²⁾Ref.[2] ³⁾Ref. [15] ⁴⁾including quantum corrections [16]

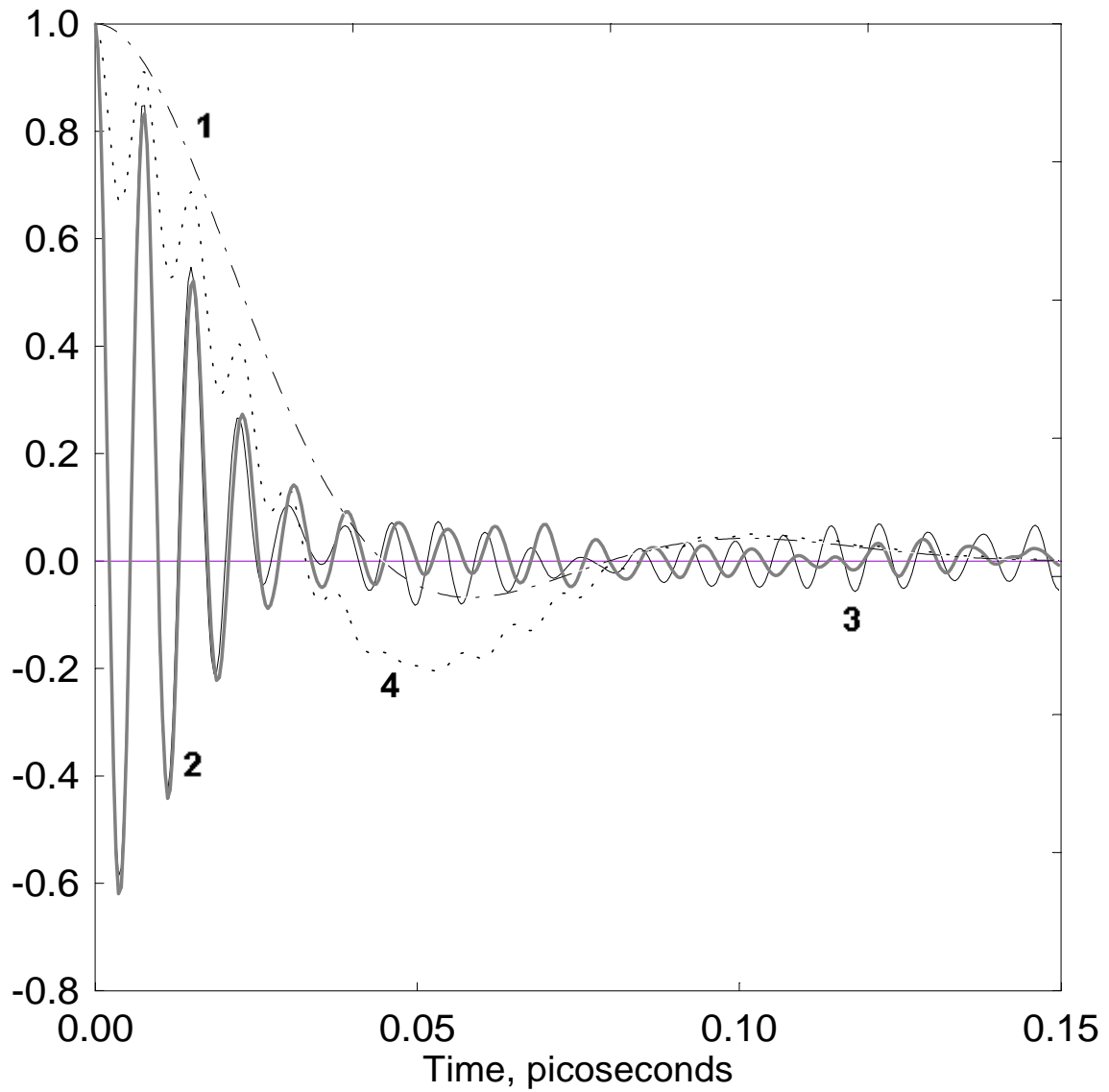


Fig.1.

Molecular (1) and atomic (2,3,4) normalized autocorrelation functions of the compressed fluid hydrogen at relatively low temperature $T=300$ K ($P=2$ GPa). The fine oscillation structure of the heat flux (thick line 2), atomic shear stress (thin solid line 3), and the velocity ACF (dot - line 4) have the same time period as the intramolecular vibration mode.

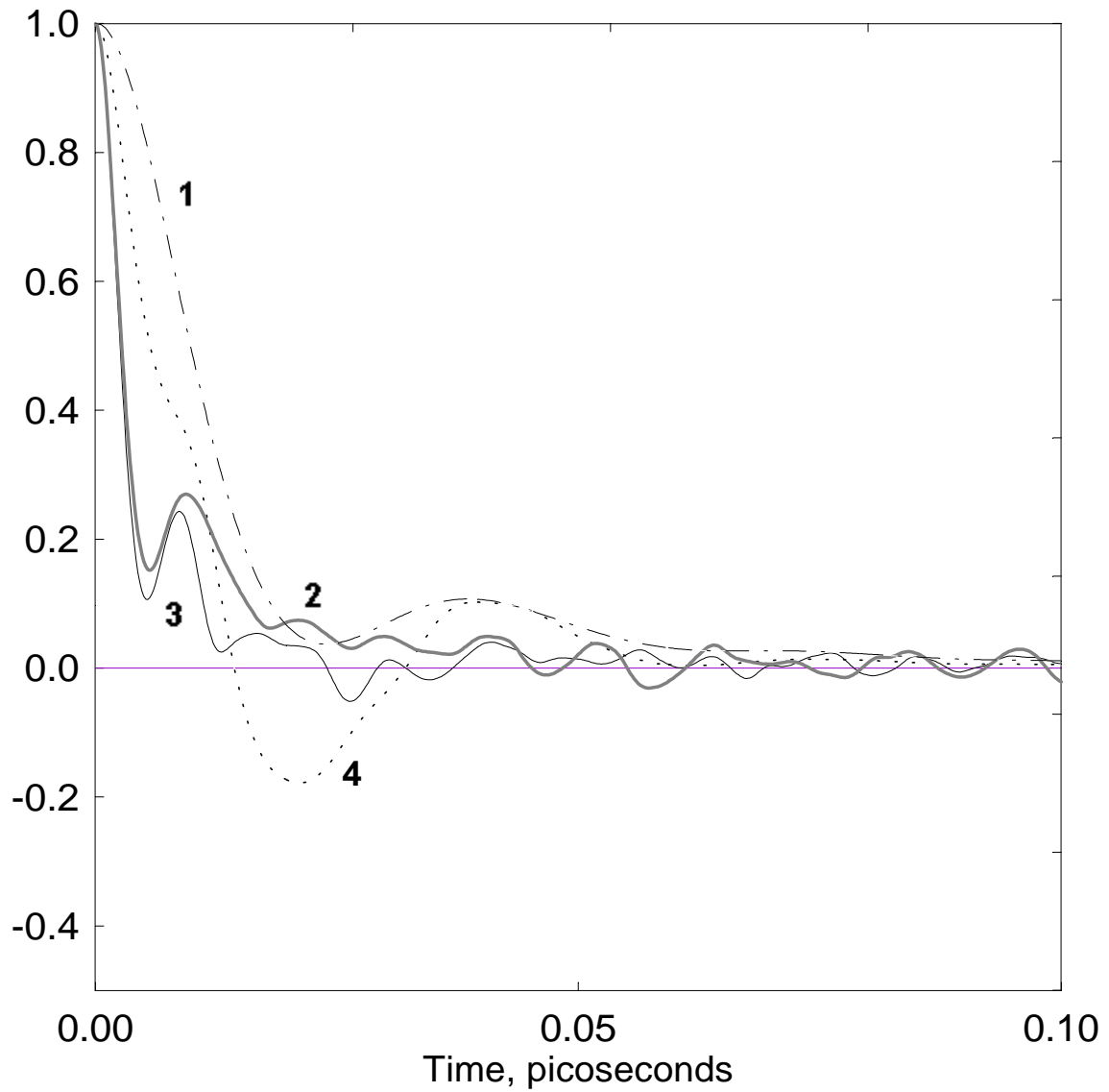


Fig.2.

ACFs in hydrogen fluid at high temperature $T=3910$ K and $P=50$ GPa fall away much faster and their oscillation structure is less pronounced than at low temperatures. The labels are the same as on Fig.1.